

ROLES AND RESPONSIBILITIES

- Simulated 1D supersonic nozzle using McCormack method for both conservative and non conservative forms of governing equations
- Conducted a grid dependence test on solution of fluid flow through nozzle
- Evaluated computation time for conservative and non conservative forms of equation for two different time steps

CODE AND RESULT SNIPPETS

the flow through that point

A) Governing Equations:

(I) Continuity Equation:

$$\frac{\partial U_1}{\partial t'} = - \frac{\partial F_1}{\partial x'}$$

(II) Momentum Equation:

$$\frac{\partial U_2}{\partial t'} = - \frac{\partial F_2}{\partial x'} + J_2$$

(III) Energy Equation:

$$\frac{\partial U_3}{\partial t'} = - \frac{\partial F_3}{\partial x'}$$

Solution vector: U

Flux vector: F

Source term: J₂

$$U_1 = \rho' A' v'$$

$$U_2 = \rho' A' v'^2$$

$$U_3 = \rho' \left(\frac{e'}{\gamma - 1} + \frac{\gamma}{2} v'^2 \right) A'$$

$$F_1 = \rho' A' v'$$

$$F_2 = \rho' A' v' + \left(\frac{1}{\gamma} \right) p' A'$$

$$F_3 = \rho' \left(\frac{e'}{\gamma - 1} + \frac{\gamma}{2} v'^2 \right) v' A' + p' A' v'$$

$$J_2 = \frac{1}{\gamma} \cdot p' \cdot \frac{dA'}{dx'}$$

(B) Initial conditions of Profile at time, t=0:

$$x(i) \geq 0.5 \text{ then } x(i) \leq 0.5$$

$$\rho(i) = 1$$

$$T(i) = 1$$

$$x(i) \geq 0.5 \text{ then } x(i) \leq 1.5$$

$$\rho(i) = 1 - 0.355 \cdot (x(i) - 0.5);$$

$$T(i) = 1 - 0.167(x(i) - 0.5);$$

$$x(i) \geq 1.5 \text{ then } x(i) \leq 3.5$$

```
function [v,rho,t,m,p,mach,v_t,rho_t,t_t,m_t,p_t,mach_t,k,time_execution_1] = non_conservative(n,x,d
x,c,gamma,a,nt,throat)
```

```
tic
```

```
% Inputs
```

```
% Length of the domain
```

```
L = 3;
```

```
% no of the grid points
```

```
n = 31;
```

```
% x array along the length of the domain
```

```
x = linspace(0,L,n);
```

```
% Grid size
```

```
dx = x(2) - x(1);
```

```
% other parameters
```

```
gamma = 1.4;
```

```
% calculate Initial profile, which are non dimensional
```

```
rho = 1-0.3146*x;
```

```
t = 1- 0.2314*x; % t =temperature
```

```
v = (0.1 + 1.09*x).*t.^0.5;
```

```
a = 1 + 2.2*(x-1.5).^2; % Area, a
```

```
% Time steps
```

```
nt = 1600
```

```
% calculating the value of time step using courant criteria
```

```
for i = 1:n
```

```
del_t(i)= c*(dx/(t(i)^0.5+v(i)));
```

```
% Inputs
```

```
% Length of the domain
```

```
L = 3;
```

```
% Number of the grid points
```

```
n = 31;
```

```
% x array along the length of the domain
```

```
x = linspace(0,L,n);
```

```
% Grid spacing
```

```
dx = x(2) - x(1);
```

```
% Area, a
```

```
a = 1+2.2*(x-1.5).^2;
```

```
gamma = 1.4
```

```
% Exact node at the throat, numbers of nodes is an odd number
```

```
throat = ((n-1)/2)+1;
```

```
% courant number
```

```
c = 0.5
```

```
% No. of time steps
```

```
nt = 1600;
```

Variation of flow parameters along x axis

